

Scattering in periodic waveguide: integral representation and spectrum decomposition

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We consider scattering problems in a periodic waveguide $\Omega = \mathbb{R} \times [0, 1]$. The problem is formulated by the following equations:

$$\Delta u + k^2 q u = f \quad \text{in } \Omega; \quad \frac{\partial u}{\partial x_2} = 0 \quad \text{on } \partial\Omega; \quad (1)$$

where q is periodic and f is compactly supported. Due to the existence of eigenvalues, the problem is not always uniquely solvable in $H^1(\Omega)$. To this end, the *Limiting Absorption Principle (LAP)* is adopted. Based on the Floquet-Bloch transform, we obtain a contour integral representation for the solution from LAP, and also decompose the solution with generalized eigenfunctions. An efficient numerical method is also developed based on that.

References

- [1] S. Fliss and P. Joly, Solutions of the time harmonic wave equation in periodic waveguides : asymptotic behaviour and radiation condition, *Arch. Ration. Mech. An.* **219(1)** (2016), pp. 349–386.
- [2] A. Kirsch and A. Lechleiter, A radiation condition arising from the limiting absorption principle for a closed full- or half-waveguide problem, *Math. Method Appl. Sci.* **41(10)** (2018), pp. 3955–3975.